

17th ILRS Workshop on Laser Ranging, Bad Kötzting, May 16-20, 2011

# **Lunar Laser Ranging - Introductory Remarks**

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# Acknowledgement

Work has been supported by

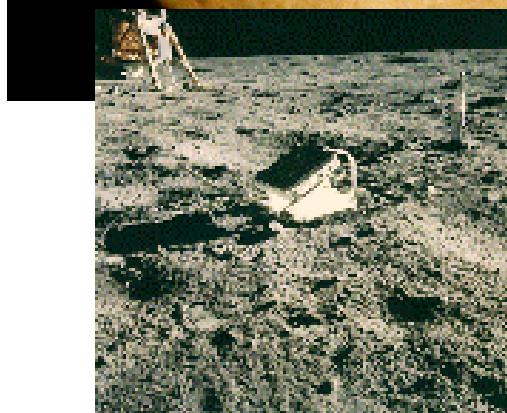
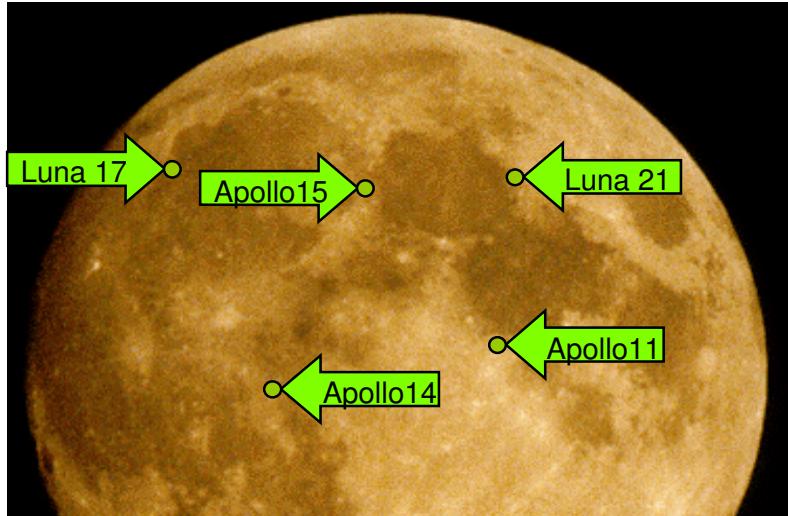


**DFG Research Unit FOR584  
Earth Rotation and Global Dynamic Processes,  
studies by Liliane Biskupek, Xing Fang**

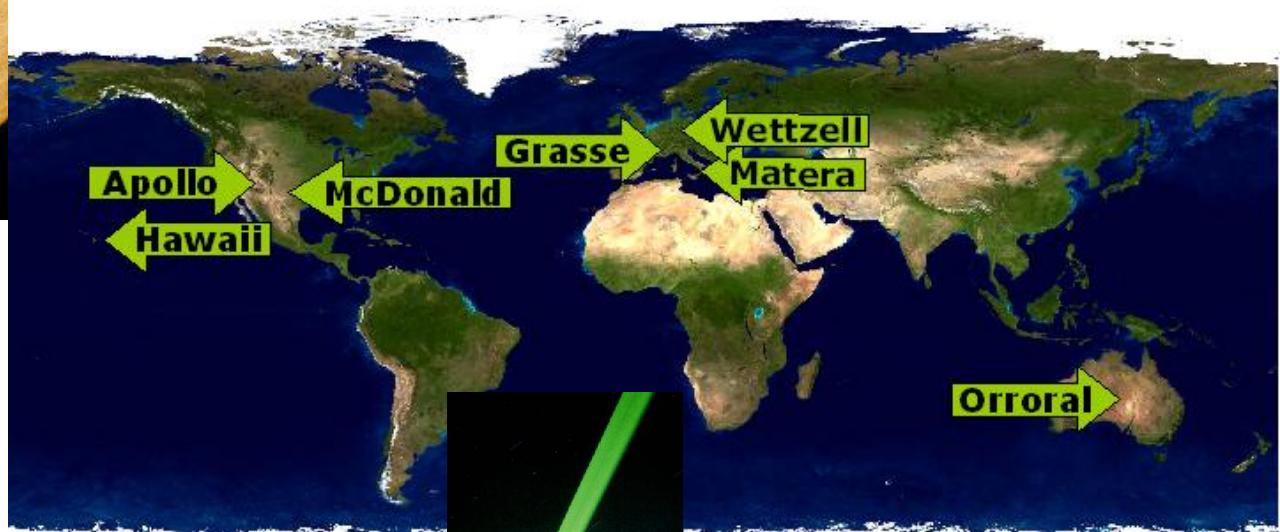


**and the Centre of Excellence QUEST  
(Quantum Engineering and Space-Time Research),  
studies by Franz Hofmann**

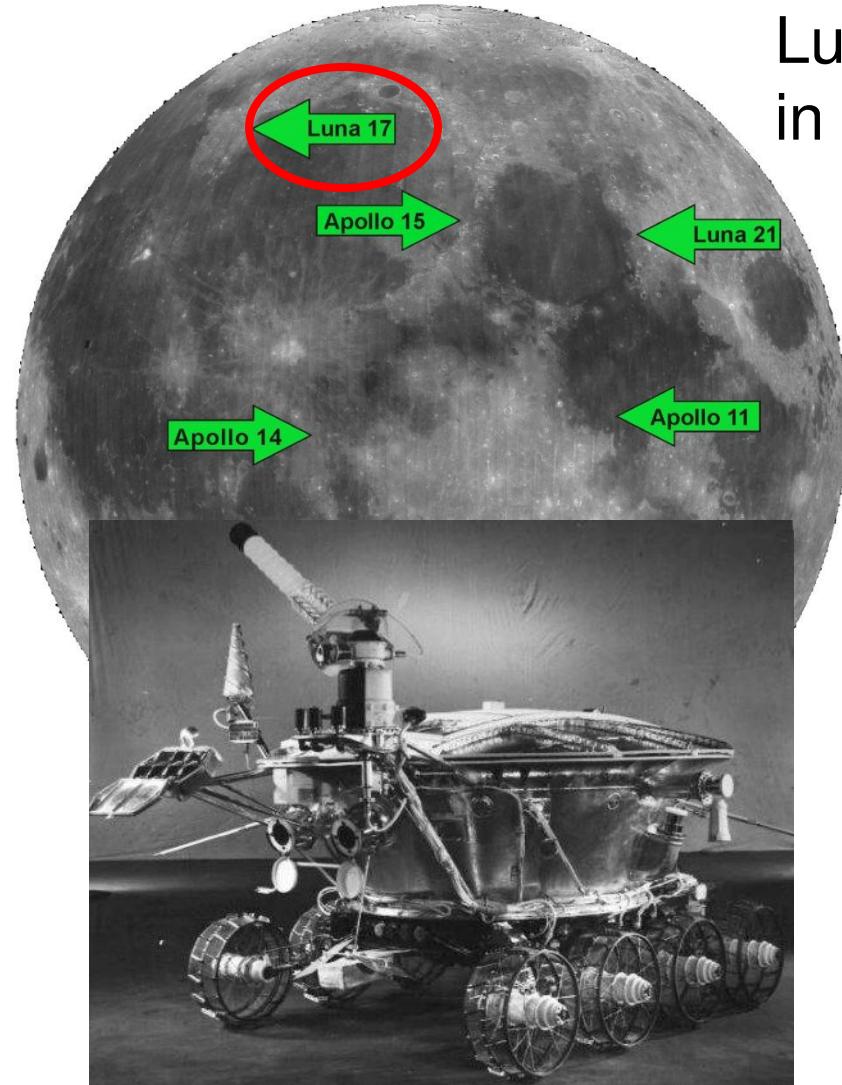
# Retro-reflectors and observatories



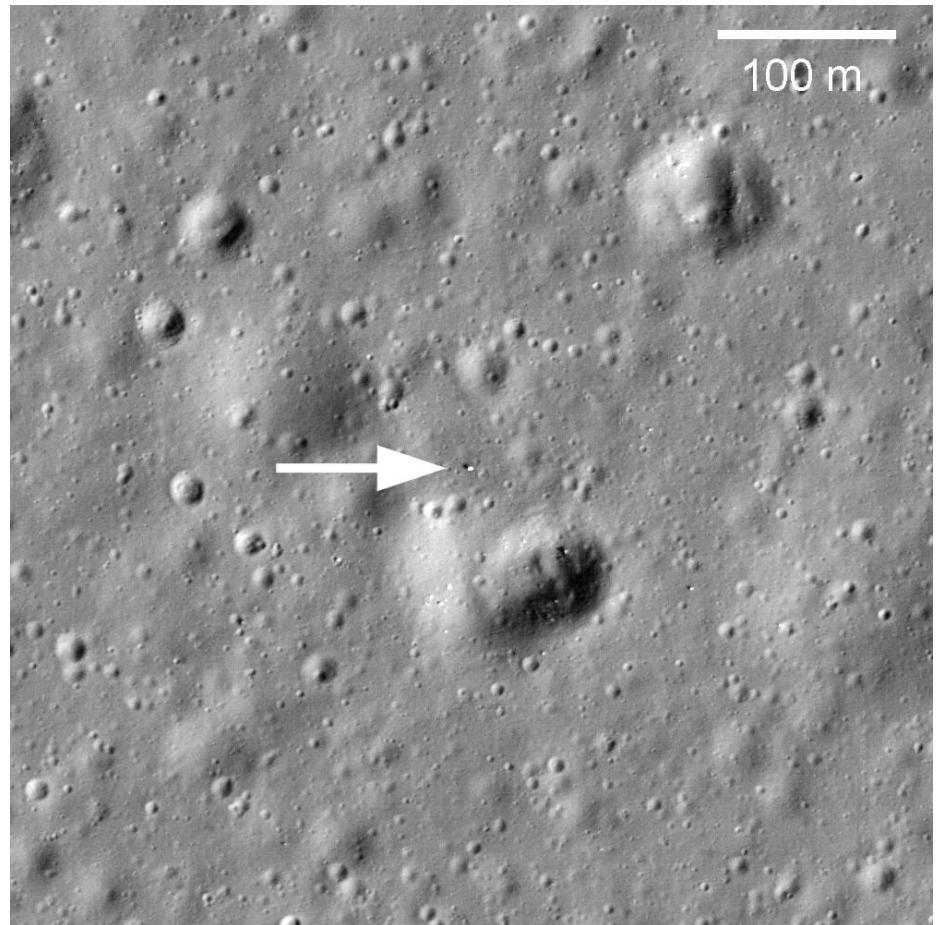
- First reflector deployed on July 21, 1969 (Apollo 11)
- “Continuous” LLR observations for 41 years



# Luna17 retro-reflector

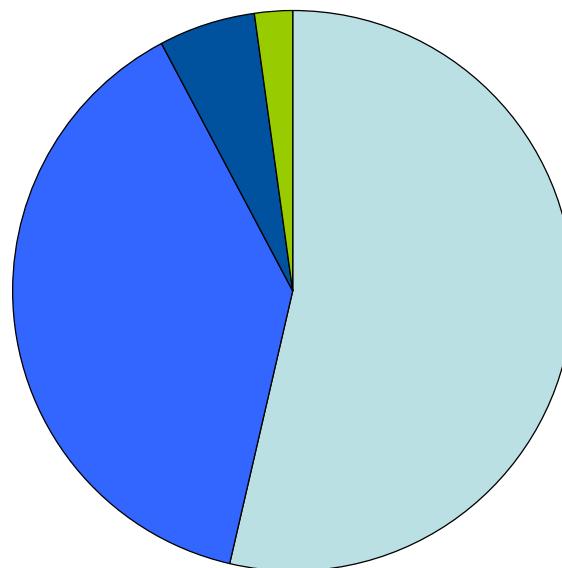
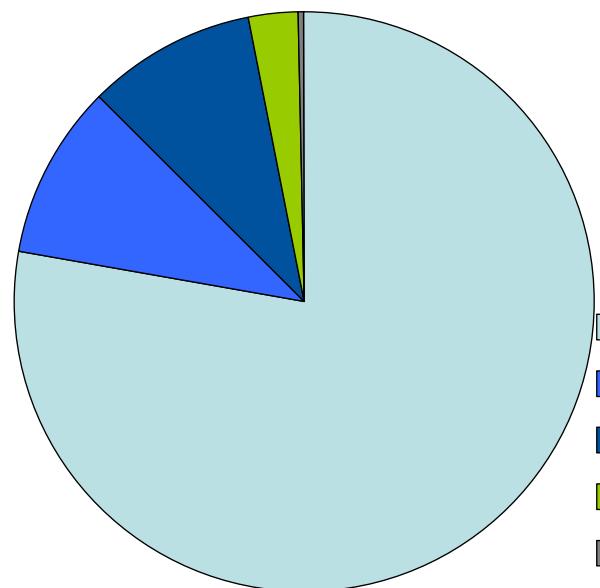


Lunokhod 1 has been re-discovered  
in April 2010



# Statistics - reflectors and observatories

Time span 1970-2011



Grasse 53.5%

McDonald 38.5%

APOLLO 5.5%

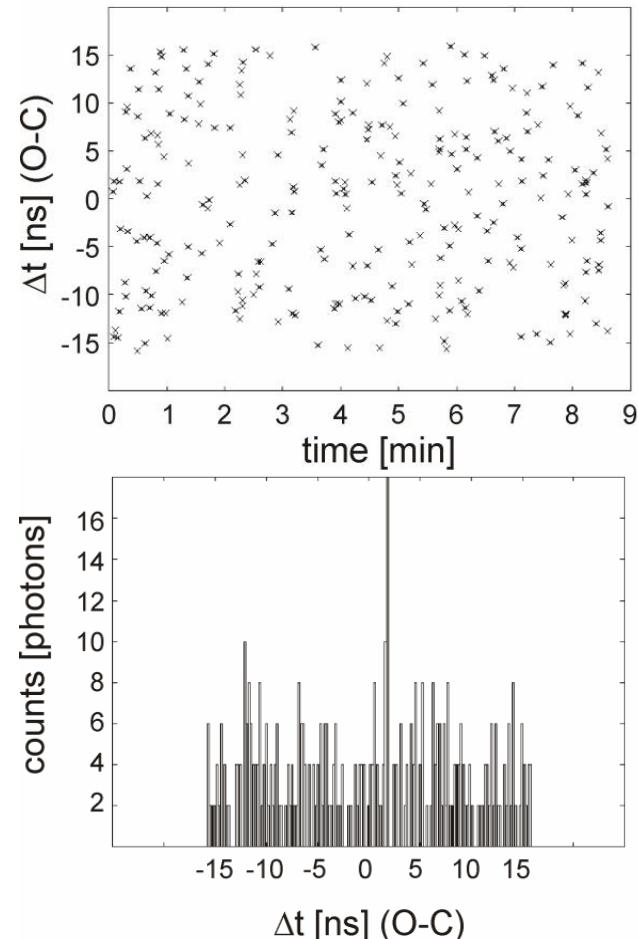
Haleakala 2.3%

... and a few lunar tracks from

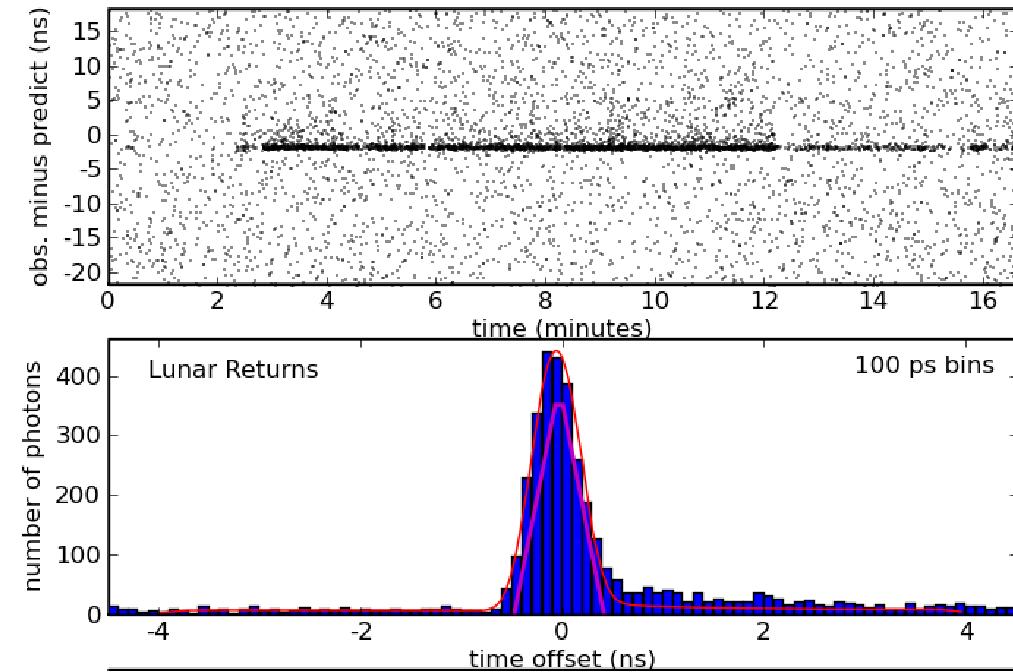
- Orroral
- Wettzell
- Matera

# LLR – returned photons

Wettzell, 0.7m telescope



APOLLO, 3.5m telescope



# Improvement of functional modelling

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Atmospheric corrections (Pavlis ...)

**Gravity field of Earth and Moon**

...

# Gravity field of Earth and Moon

Already implemented (Newtonian modelling)

- Translation:

$$\text{Earth } Y_{2-4}^0 \leftrightarrow \text{Moon } Y_0^0$$

$$\text{Moon } Y_{2-4}^{0-4} \leftrightarrow \text{Earth } Y_0^0$$

$$\text{Earth } Y_2^0 \leftrightarrow \text{Sun } Y_0^0$$

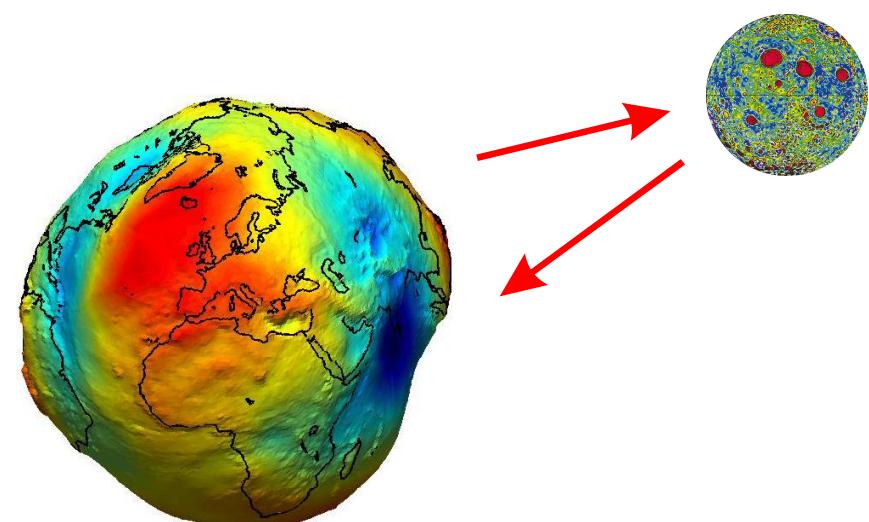
$$\text{Moon } Y_2^{0-2} \leftrightarrow \text{Sun } Y_0^0$$

- Rotation:

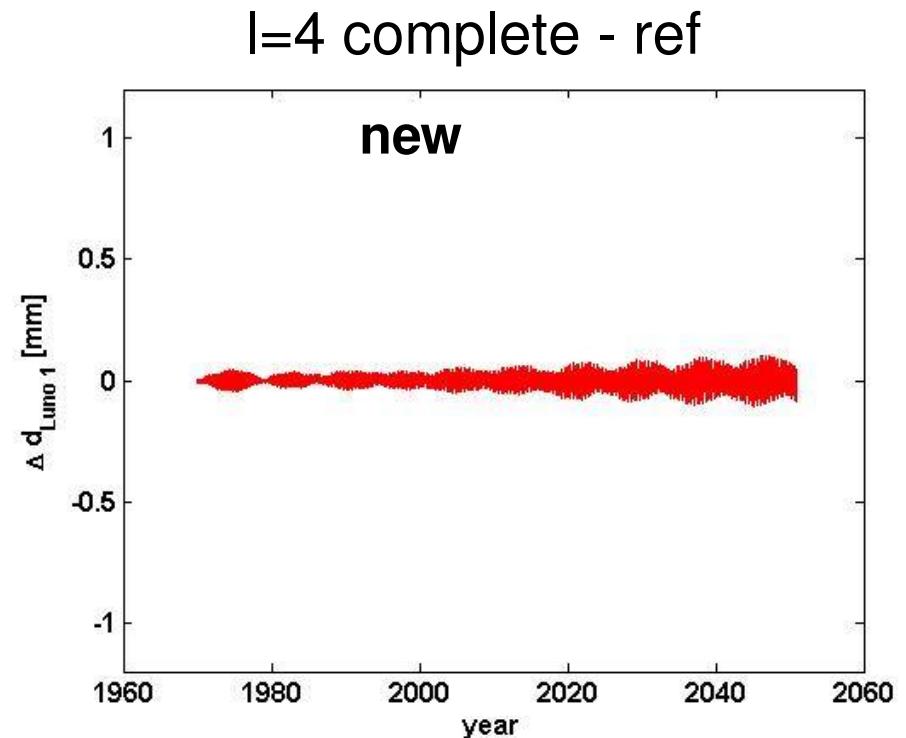
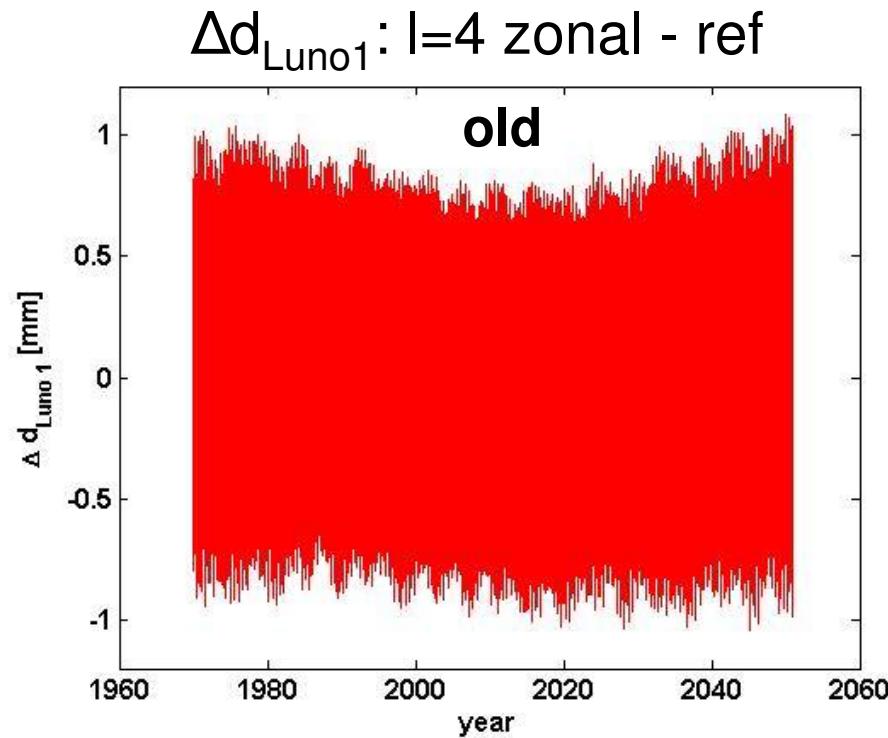
$$\text{Earth } Y_0^0 \rightarrow \text{Moon } Y_{2-4}^{0-4}$$

$$\text{Sun } Y_0^0 \rightarrow \text{Moon } Y_{2-4}^{0-4}$$

$$\text{Earth } Y_2^{0-2} \rightarrow \text{Moon } Y_2^{0-2}$$



# Case: Earth 4 zonal → 4 complete

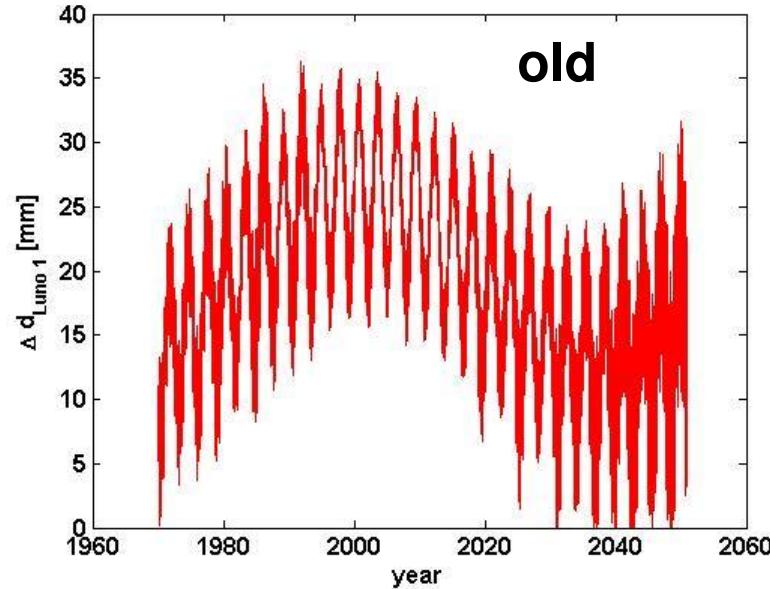


$$\Delta d_{\text{Luno1}} = d_{\text{Luno1\_comp}} - d_{\text{Luno1\_ref}}$$

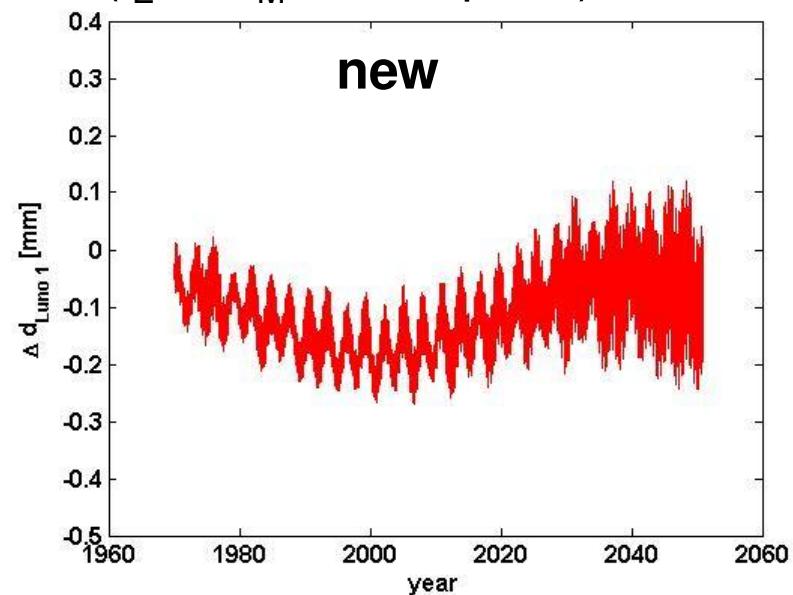
Note: time consuming computation in ephemeris program

# Case: Earth + Moon, Luno 1 distance

$\Delta d_{\text{Luno1}}$ : ( $I_E=4$  zonal,  $I_M=4$  complete) - ref



( $I_E=4$ ,  $I_M=5$  complete) - ref



- Difference is dominated by lunar gravity field

# Improvement of stochastic modelling

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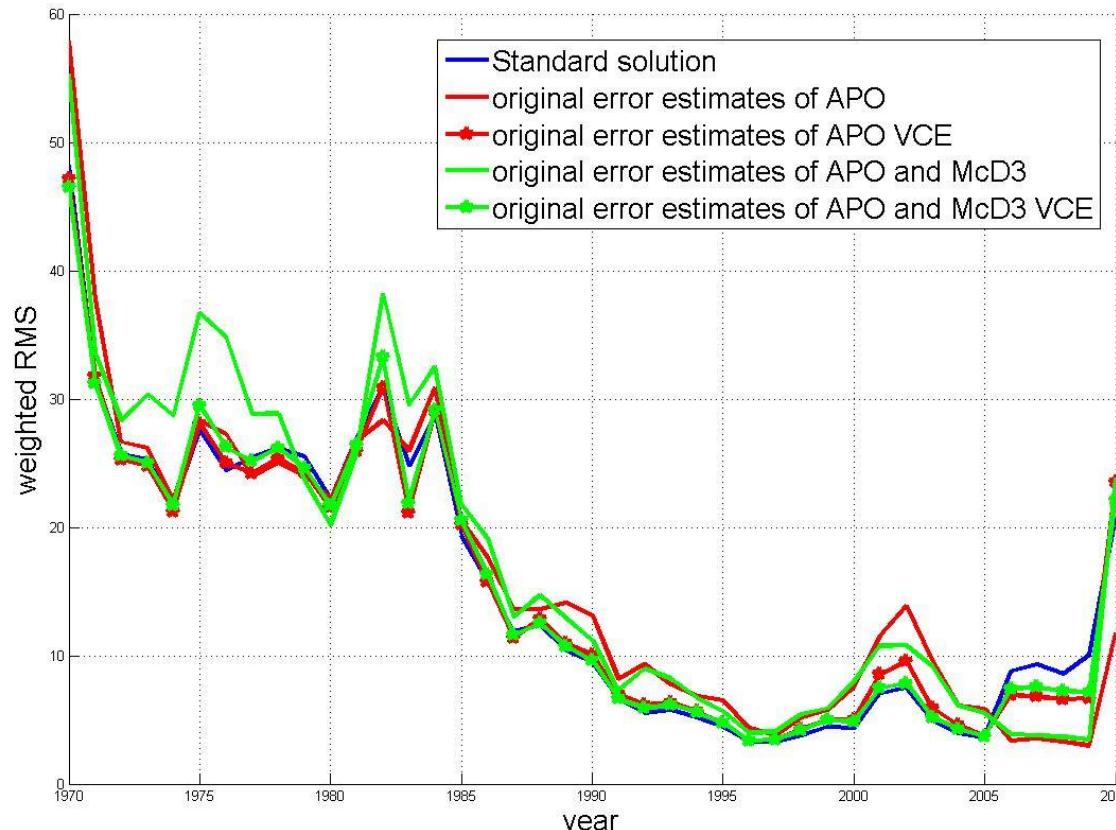
Variance component estimation

Eigenvalue decomposition

Outlier testing

# VCE result

Standard solution compared to solutions based on original error estimates from APO resp. from APO and McD3, solutions based on original error estimates plus applying VCE.



# New Results

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Standard solution

- new reflector (Lunakhod 1)
- new sites (Matera)

**Relativistic parameters**

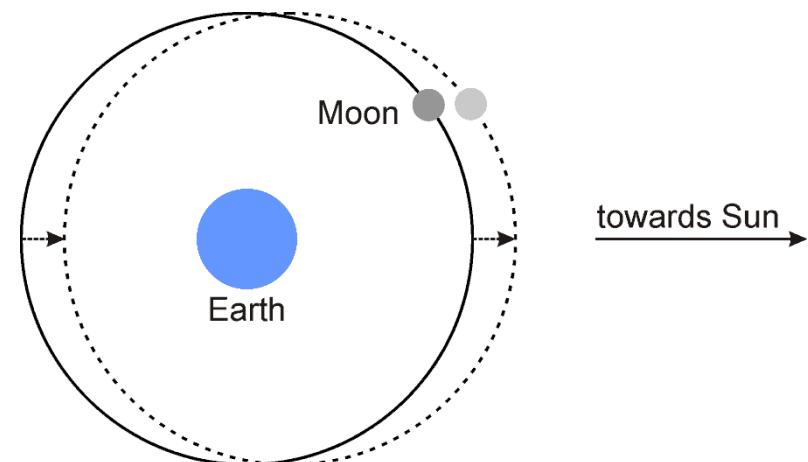
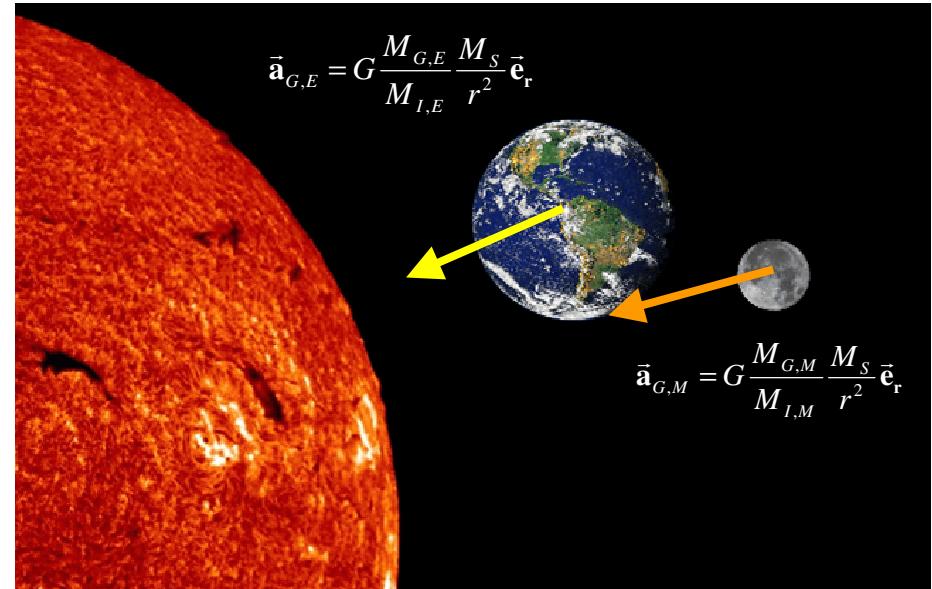
# Equivalence principle test with LLR

- Earth Moon values:

$$\left( \frac{U}{Mc^2} \right)_{Earth} = -4.64 \times 10^{-10}$$

$$\left( \frac{U}{Mc^2} \right)_{Moon} = -1.90 \times 10^{-11}$$

- If  $\eta \neq 0$ 
  - Different accelerations
  - Polarisation of lunar orbit
- LLR best technique for lunar orbit determination  
→ use Earth-Moon system for testing SEP violation



# LLR tests of general relativity

Temporal variation of the gravitational constant

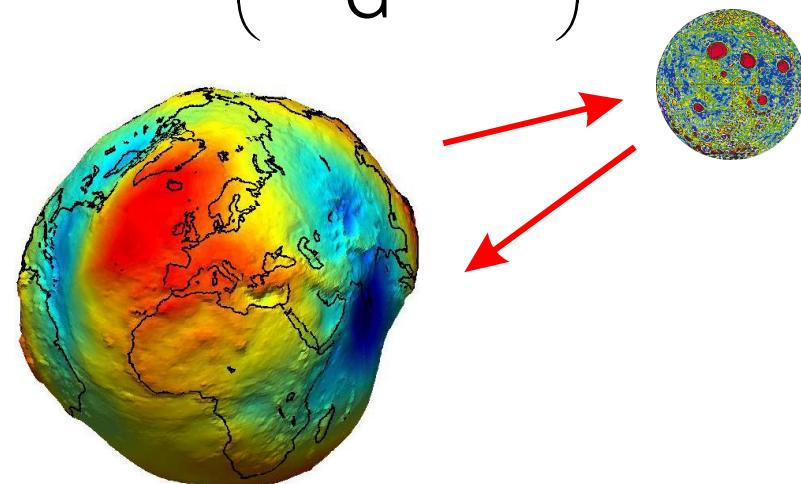
$$\frac{\dot{G}}{G} = (1 \pm 4) \cdot 10^{-13} \text{ yr}^{-1}$$

$$G = G_0 \left( 1 + \frac{\dot{G}}{G} \Delta t + \dots \right)$$

Strong equivalence principle

$$\eta = (1 \pm 5) \times 10^{-4}$$

$$\left[ \frac{M_G}{M_I} \right]_{SEP} - 1 = (-0.5 \pm 2.3) \times 10^{-13}$$



**Factor 2 improvement due to  
refined modelling and more LLR data**

Hofmann, Müller, Biskupek,  
Astron. & Astroph., 2010

# Further activities

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ISSI workshop series on LLR modelling and analysis  
(start 2009)

Boston workshop 2010 on comparison of LLR software packages

ILRS initiative on LLR data qualification

DFG Research unit “Reference systems”  
(speaker A. Nothnagel, Bonn)  
• Moon related systems  
• Barycentric ephemeris

# Requirements for LLR data qualification?

## Criteria for tracking (new) LLR sites

- number of reflector arrays to be observed:  
**at least Apollo15, then LK1, the others if possible**
- successful observation days/nights per month: **1 - 4**
- normal points per year: (**~12 to Ap15**), but try **100**
- normal point accuracy: **< 0.1 ns** (goal **< 0.05 – 0.01 ns**)
- post-fit residual of single NP to global solution: **< 1 ns**

## LLR website

- General rules: tracking and further ILRS criteria
- Checking quality of LLR data (Paris website  
<http://polac.obspm.fr/PaV>)

# Conclusions

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## Ongoing activities

- Improved functional and stochastic modelling
- Work on refined LLR data analysis
- Qualification/comparison of data and analysis  
(exchange in LLR community)

## Future steps

- Enhanced studies on lunar interior, earth rotation and relativity
- New LLR experiments (transponders ...)